

# DISTANCES IN THE UNIVERSE

How to interpret data from databases and how to calculate the distance of galaxies from redshift measurements



# LOCALIZING THE OBJECT OF INTEREST

PGC2432563

(Name of the object, from PixInsight Annotation)

+ some additional  
Deconvolution & Denoising



SimBAD search to get the coordinates

<https://simbad.cds.unistra.fr/simbad/>



NED search to get information about the object

<https://ned.ipac.caltech.edu/>



Results for object WISEA J113253.44+530749.0

Overview | Cross-IDs (10) | Coordinates (8) | Redshifts (3) | Distances (0) | Classifications (0) | Galactic Extinctions | Notes (0) | Diameters (8)

Photometry & SED (55) | Spectra (1) | Images (0) | References (11) | External Links | Survey Coverage

POSS-II F (North), AAO-SES/SERC-ER (South), Red image  
View in IRSA Finderchart  
Image Credit: Caltech or AAO/ROE

Selected data and derived quantities for WISEA J113253.44+530749.0. More information in the tabs above.

Cross-identifications		Essential note			
WISEA J113253.44+530749.0; 2MASX J11325338+5307491; SDSS J113253.40+530748.8; SDSS J113253.40+530749.0; SDSS J113253.41+530749.0					
Coordinates for Fiducial Position					
Equatorial (J2000)					
RA, Dec	RA, Dec [Deg]	Unc Semi-major, minor ["]	Unc PA [deg]	Reference	Galactic
11h32m53.4486s, +53d07m49.019s	173.222702, 53.130283	0.15400, 0.14900	0	2013wise_rept....1C	146.864601, 1
Fiducial Redshift & Derived Quantities [ $H_0 = 67.8$ km/sec/Mpc, $\Omega_{matter} = 0.308$ , $\Omega_{vacuum} = 0.692$ ]					
z (Helio)	cz (Helio) [km/s]	Reference	cz (CMB) [km/s]	Hubble Distance (CMB) [Mpc]	Mean Distance
0.178061 ± 1.67e-5	53381 ± 5	2023arXiv230606308D	53565 ± 14	790.05 ± 55.30	N/A ± N/A
Classifications					
Object Type	Morphology	Reference	Activity Type	Reference	Other
G					
Quick-look Angular & Physical Diameters			Foreground Galactic Extinction (2011A)		
Passband	Diameter ["]	Reference	Diameter* [kpc]	$A_V$ [mag] Landolt V	$A_V$ [mag] UKIRT
r (SDSS Isophotal)	16.43	2007SDSS6C...0000:	62.97	0.037	0.004

\*Derived physical diameter is based on the Hubble flow distance corrected for (Virgo + GA = Shapley) = 790.41 Mpc

# OBJECT DATA from NED

What are derived quantities???

What the hell does  
all these numbers  
mean?



PGC2432563 / WISEA J113253.44+530749.0



Results for object WISEA J113253.44+530749.0

Overview | Cross-IDs (10) | Coordinates (8) | Redshifts (3) | Distances (1) | Classifications (0) | Galactic Extinctions | Notes (0) | Diameters (8)

Photometry & SED (55) | Spectra (1) | Images (0) | References (1) | Survey Coverage

POSS-II F (North), AAO-SES/SERC-ER (South), Red image  
[View in IRSA Finderchart](#)  
Image Credit: Caltech or AAO/ROE

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Coordinates for Fiducial Position					
Equatorial (J2000)					
RA, Dec	RA, Dec [Deg]	Unc Semi-major,minor ["]	Unc PA [deg]	Reference	Galactic Lon, Lat [deg]
11h32m53.4486s, +53d07m49.019s	173.222702, 53.130283	0.15400, 0.14900	0	2013wise.rept....1C	146.864601, 4...
Fiducial Redshift & Derived Quantities [ $H_0 = 67.8$ km/sec/Mpc, $\Omega_{\text{matter}} = 0.308$ , $\Omega_{\text{vacuum}} = 0.692$ ]					
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Object Type	Morphology	Reference	Activity Type	Reference	Other
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Passband	Diameter ["]	Reference	Diameter <sup>*</sup> [kpc]	$A_{\lambda}$ [mag] Landolt V	$A_{\lambda}$ [mag] UKID
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# EXPLANATION OF THE NED TABLE DATA

Cross-identifications	Essential note
WISEA J113253.44+530749.0; 2MASS J11325338+5307491; SDSS J113253.40+530748.8; SDSS J113253.40+530749.0; SDSS J113253.41+530749.0	

**Cross-identifications** = *WISEA J113253.44+530749.0*

A list of alternative names or catalog entries for the same astronomical object across different surveys and databases

Coordinates for Fiducial Position					Galactic
Equatorial (J2000)					
RA, Dec	RA, Dec [Deg]	Unc Semi-major,minor ["]	Unc PA [deg]	Reference	Lon, Lat [deg]
11h32m53.4486s, +53d07m49.019s	173.222702, 53.130283	0.15400, 0.14900	0	2013wise.rept....1C	146.864601,

## Coordinates for Fiducial Position

The Fiducial Position refers to the reference sky coordinates used to define the exact location of an object in the sky — usually given in a standard celestial coordinate system (Equatorial J2000)

RA, Dec = *11h32m53.4486s, +53d07m49.019s*  
Right Ascension (RA) and Declination (DEC) Coordinates

RA, Dec [Deg] = *173.222702, +53.130283*  
Coordinates on the celestial sphere

UNC Semi-major, minor = *0.15400, 0.14900*  
Uncertainties of the measured size and shape – specifically its ellipse-like shape.

$$24h = 360^\circ, \rightarrow 1h = 15^\circ$$

**Example**

$$RA (Deg) = 11 \cdot 15^\circ + \frac{32}{60} \cdot 15^\circ + \frac{53.4486}{3600} \approx 173.2227^\circ$$

# EXPLANATION OF THE NED TABLE DATA

Fiducial Redshift & Derived Quantities [ $H_0 = 67.8$ km/sec/Mpc, $\Omega_{\text{matter}} = 0.308$ , $\Omega_{\text{vacuum}} = 0.692$ ]					Redshift-ind
z (Helio)	cz (Helio) [km/s]	Reference	cz (CMB) [km/s]	Hubble Distance (CMB) [Mpc]	Mean Distanc
$0.178061 \pm 1.67e-5$	$53381 \pm 5$	<a href="#">2023arXiv230606308D</a>	$53565 \pm 14$	$790.05 \pm 55.30$	N/A $\pm$ N/A

## Fiducial Redshift & Derived Quantities [ $H_0 = 67.8$ km/sec/Mpc, $\Omega_{\text{matter}} = 0.308$ , $\Omega_{\text{vacuum}} = 0.692$ ]

$z\text{-Helio} = 0.178061 \pm 1.67e-5$  (**Measured!!**)

The redshift of the galaxy relative to the Sun (heliocentric frame). Measures how much the light was stretched by the expansion of the Universe.

$c_z$  (Helio) [km/s] =  $53381 \pm 5$  (**calculated**)

Recession velocity (in km/s), calculated by multiply the speed of light with the measured redshift, relative to the Sun

Reference = [2023arXiv230606308D](#)

The paper or catalog where this redshift measurement was published.

$c_z$  (CMB) [km/s] =  $53565 \pm 14$  (**calculated**)

Velocity of the galaxy relative to the cosmic microwave background (CMB).  $c_z(\text{CMB})$  is a corrected version of  $c_z(\text{Helio})$ , compensating for the motion of the Earth and Solar System relative to the CMB.

Hubble Distance (CMB) [Mpc] =  $790.05 \pm 55.30$  (**calculated**)

The comoving distance is derived from the Friedmann–Lemaître–Robertson–Walker (FLRW) metric by integrating over redshift using a cosmological model with specified parameters (e.g.  $H_0$ ,  $\Omega_{\text{matter}}$ ,  $\Omega_{\text{vacuum}}$ ). At low redshifts, this reduces to Hubble's law, which provides a good approximation when the expansion of the Universe hasn't changed significantly over time.

### Example

$$c_z = 299792.458 \frac{\text{km}}{\text{s}} \cdot 0.178061 \approx 53381 \frac{\text{km}}{\text{s}}$$

Hubble's law  $D_c \approx \frac{c_z}{H_0}$

# EXPLANATION OF THE NED TABLE DATA

Classifications					
Object Type	Morphology	Reference	Activity Type	Reference	Other
G					

## Classification = *G*

This is a broad classification indicating that the object is confirmed to be a galaxy — but no specific subtype (like spiral, elliptical, irregular, or AGN) is assigned (yet).

Quick-look Angular & Physical Diameters				Foreground Galactic Extinction (2011A)	
Passband	Diameter ["]	Reference	Diameter† [kpc]	A <sub>λ</sub> [mag] Landolt V	A <sub>λ</sub> [mag] UKIRT
r (SDSS Isophotal)	16.43	2007SDSS6.C...0000:	62.97	0.037	0.004

†Derived physical diameter is based on the Hubble flow distance corrected for (Virgo + GA + Shapley) = 790.41 Mpc

## Quick-look Angular & Physical Diameters

Angular Diameter = 16.43"

tells you how big the object appears on the sky – measured in arcseconds (")

Physical Diameter = 62.97

the true size of the galaxy – in kiloparsecs (kpc) – calculated from the angular size and the galaxy's distance using the angular diameter distance

$$D_{phys} = \theta \cdot D_a$$

### Example

$D_a = 790 \text{ Mpc}$  (Hubble Distance),  $D_{arcsec} = 16.43''$

$$\theta = \frac{\pi}{180} \cdot \frac{D_{arcsec}}{3600} = 7,96549 \cdot 10^{-5}$$

$$D_{phys} = 7,96549 \cdot 10^{-5} \cdot 790 \text{ Mpc} = 0,06292 \text{ Mpc} = 62.9 \text{ kpc}$$



# HOW DISTANCES ARE CALCULATED

**Hubble's law** is a simple linear relation used to estimate distances for nearby galaxies, where the expansion of the Universe hasn't changed significantly over time. The redshift should be small, typically  $< 0.1$

$$\text{Hubble's law} \quad D_c \approx \frac{c z}{H_0}$$

For galaxies at moderate to high redshifts, the Universe's expansion rate has changed significantly due to the influence of matter and dark energy. In this case, we use the **Comoving Distance Formula**, which is derived from the **Friedmann–Lemaître–Robertson–Walker (FLRW) metric** and a cosmological model.

The most commonly used model is the **Lambda-CDM model**, which will be described on the next slides

# THE LAMBDA-CDM MODEL ( $\Lambda$ CDM)

## Key Assumptions of the $\Lambda$ CDM

- 1 The universe is homogeneous and isotropic on large scales

Means, it looks the same in all directions and locations!

- 2 The expansion and structure of the Universe is described by Einstein's field equations

$$G_{\mu\nu} + \Lambda g_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}$$

**Tells spacetime how to curve**  
(Curvature of space time)

**Describes what is in it**  
(Matter and energy)



# THE LAMBDA-CDM MODEL ( $\Lambda$ CDM)

## Key Assumptions of the $\Lambda$ CDM – Part 2

### 3 The geometry of the universe is flat

That means, that the energy density parameter  $\Omega$  is equal to 1.

$$\Omega = \Omega_m + \Omega_r + \Omega_\Lambda = 1$$

$\Omega_m$  = Matter Density Parameter

Describes the fraction of the total energy density of the Universe made of matter

→ **Baryonic matter** like stars, gas, atoms

→ **Cold dark matter**

$\Omega_r$  = Radiation Density Parameter

Fraction of the Universe's total energy density made of radiation

→ **Photons from CMB (Comic Microwave Background)**

$\Omega_\Lambda$  = Dark Energy Density Parameter

Fraction of the Universe's total energy density made of dark energy

Measurements have shown that we live in a really flat universe!

$$\Omega \approx 1.000 \pm 0.005$$



# THE LAMBDA-CDM MODEL ( $\Lambda$ CDM)

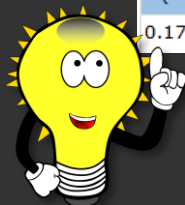
## Key Assumptions of the $\Lambda$ CDM – Part 3

### 4 The Universe consists of

- ~5% Baryonic matter (normal matter like atoms, gases, matter like you and me)
- ~25% Cold dark Matter (**CDM**)
- ~70% Dark Energy ( $\Lambda$ )

Here, we can find the first parameters from our NED table !!!

Fiducial Redshift & Derived Quantities [ $H_0 = 67.8$ km/sec/Mpc, $\Omega_{matter} = 0.308$ , $\Omega_{vacuum} = 0.692$ ]				Redshift-independent	
z (Helio)	cz (Helio) [km/s]	Reference	cz (CMB) [km/s]	Hubble Distance (CMB) [Mpc]	Mean Distance
$0.178061 \pm 1.67e-5$	$53381 \pm 5$	<a href="#">2023arXiv230606308D</a>	$53565 \pm 14$	$790.05 \pm 55.30$	N/A $\pm$ N/A



$$\Omega_{matter} = 0.308 = \Omega_{Baryonic} + \Omega_{CDM}$$

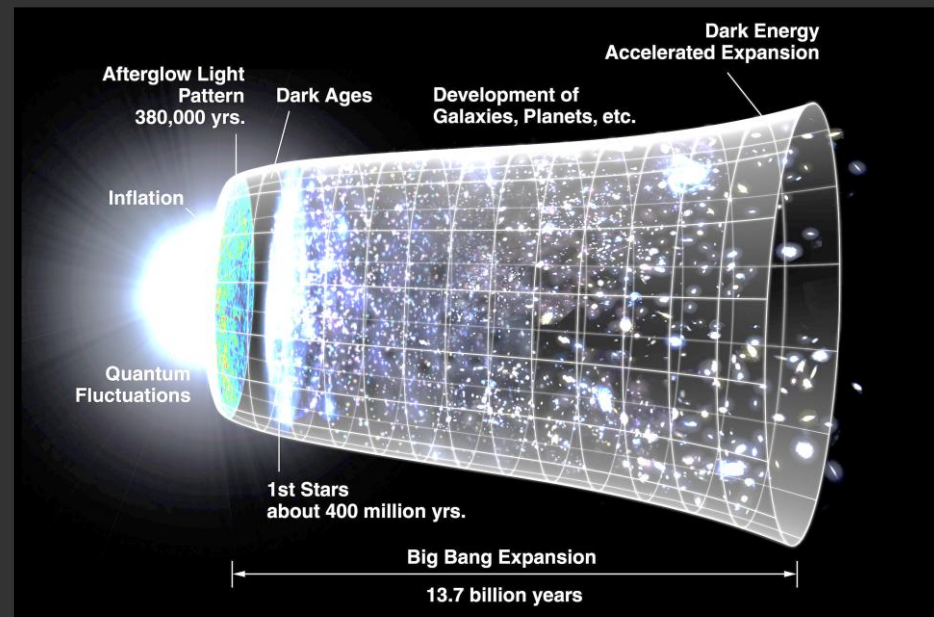
$$\Omega_{vacuum} = 0.692 = \Omega_{\Lambda}$$

$$\Omega_{\gamma} = 0.00005 \rightarrow \text{negligible and not shown}$$

# THE LAMBDA-CDM MODEL ( $\Lambda$ CDM)

## Key Assumptions of the $\Lambda$ CDM – Part 4

- 5 **Inflation** – The early Universe expanded extremely rapidly, and tiny quantum fluctuations during this phase became the seeds of all large-scale structures we observe today



# CALCULATION OF THE DISTANCE

The parameters shown in the **NED Table** can be used to calculate the distance and recession velocity

Fiducial Redshift & Derived Quantities [ $H_0 = 67.8$ km/sec/Mpc, $\Omega_{\text{matter}} = 0.308$ , $\Omega_{\text{vacuum}} = 0.692$ ]		
z (Helio)	cz (Helio) [km/s]	Reference
$0.178061 \pm 1.67e^{-5}$	$53381 \pm 5$	2023arXiv230606308D

$$z = 0.178061 \pm 1.67e^{-5}$$

(Red Shift measurement)

$$H_0 = 67.8 \frac{\text{km/s}}{\text{Mpc}}$$

(Hubble constant)

$$\Omega_m = 0.308$$

(Matter density)

$$\Omega_\Lambda = 0.692$$

(Dark energy density)

These parameters are used in the **Comoving Distance Integral** to calculate the distance to the galaxy

$$D_c(z) = \frac{c}{H_0} \int_0^z \frac{dz'}{E(z')} \quad \text{(simplified Comoving Distance Formula)}$$

# CALCULATION OF THE DISTANCE

The **Comoving Distance Formula** is an extraction derived from the **Friedmann–Lemaître–Robertson–Walker (FLRW) metric**

$$D_c(z) = \frac{c}{H_0} \int_0^z \frac{dz'}{E(z')} \quad \text{with}$$

$$H_0 = 67.8 \frac{\text{km/s}}{\text{Mpc}} \text{ (Hubble constant)}$$

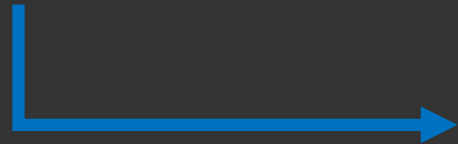
$$c = 299792.458 \frac{\text{km}}{\text{s}} \text{ (Speed of light)}$$

$z$  = measured redshift

$E(z')$  = normalized Hubble parameter

Since we assume a flat Universe ( $\Omega = 1$ ) and we negligible the energy density of

radiation  $E(z) = \sqrt{\Omega_m(1+z)^3 + \Omega_\Lambda}$



$$D_c(z) = \frac{c}{H_0} \int_0^z \frac{dz'}{\sqrt{\Omega_m(1+z)^3 + \Omega_\Lambda}}$$

**Comoving Distance Formula**

# CALCULATION OF THE DISTANCE

## When we now calculate the Comoving Distance by using a little Python Script

### Python Script to calculate the Comoving Distance

```
import numpy as np
from scipy.integrate import quad

# Constants
H0 = 67.8 # Hubble constant in km/s/Mpc
c = 299792.458 # Speed of light in km/s
Ωm = 0.308
ΩΛ = 0.692

# Define E(z) based on the Lambda-CDM model
def E(z):
    return np.sqrt(Ωm * (1 + z)**3 + ΩΛ)

# Define the integrand for the comoving
distance integral
def integrand(z):
    return 1.0 / E(z)

# Upper limit of integration (redshift
measurement)
z_max = 0.178061

# Perform the integration
integral, _ = quad(integrand, 0, z_max)

# Calculate comoving distance
D_C = (c / H0) * integral
D_C
```

### Example

$$D_c(z) = \frac{c}{H_0} \int_0^z \frac{dz'}{\sqrt{\Omega_m(1+z')^3 + \Omega_\Lambda}}$$

with

$$H_0 = 67.8 \frac{\text{km/s}}{\text{Mpc}} \text{ (Hubble constant)} \quad c = 299792.458 \frac{\text{km}}{\text{s}} \text{ (Speed of light)}$$

$z = 0.178061$  (the redshift measurement from the NED Database)

Comoving Distance  $D_c(z) = 754.03 \text{Mpc}$

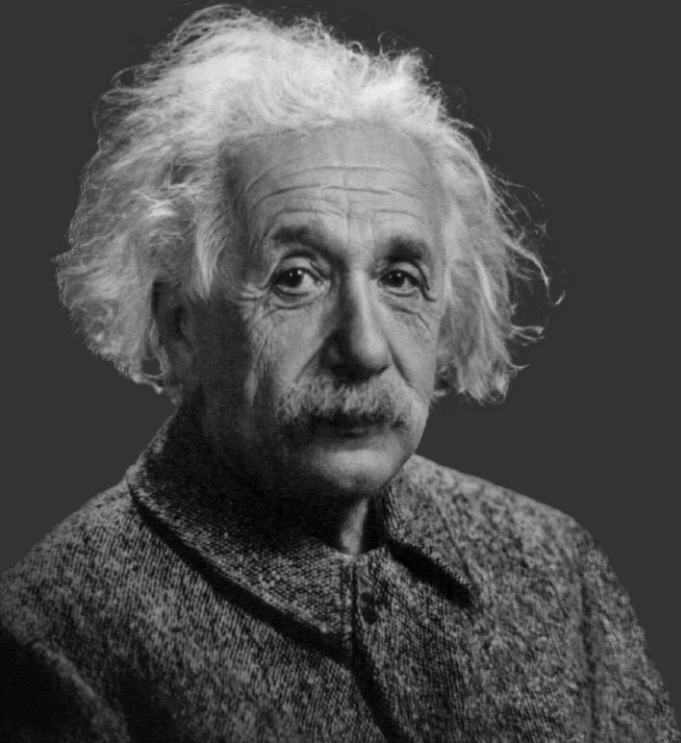
# SUMMARIZED IN SIMPLE WORDS

1. We observe the light from a distant galaxy using a spectrometer and notice that it is redshifted – meaning the wavelength has been stretched due to cosmic expansion
2. The redshift tells us how long the light has been traveled – the higher the redshift, the farther away the galaxy is!
3. Due to the fact that the Universe hasn't expanded at a constant rate ( $\rightarrow$  *Inflation*), we need to account for how fast the Universe was expanding each moment in time.
4. We divide the light's journey into many small steps and calculate how far the light traveled in each step, based on the universe's expansion rate at that redshift.
5. Finally, we add up all these little steps which gives us the comoving distance  $\rightarrow$  the present-day distance to the galaxy accounting the expansion of the universe over time



# SUMMARIZED IN SIMPLE WORDS

We calculate how far the light had to travel to reach us  
today, taking into account how the expansion of the  
Universe changed along the way



Thank you,  
**Albert Einstein**

*\*14.03.1879 † 18. April 1955*

# WHAT DOES THAT MEAN FOR OUR GALAXY?

Name: *WISEA J113253.44+530749.0*



$$z\text{-Helio} = 0.178061 \pm 1.67e-5$$

$$c_z \text{ (Helio)} \text{ [km/s]} = 53381 \pm 5 \quad \rightarrow$$

$$c_{z,\text{helio}} = c \cdot z = 299792.458 \frac{\text{km}}{\text{s}} \cdot 0.178061 \approx 53381 \frac{\text{km}}{\text{s}}$$

$$c_z \text{ (CMB)} \text{ [km/s]} = 53565 \pm 14 \quad \rightarrow$$

$$c_{z,\text{CMB}} = c_{z,\text{helio}} + v_{\text{corr}} = 53381 \frac{\text{km}}{\text{s}} + 184 \frac{\text{km}}{\text{s}} \approx 53565 \frac{\text{km}}{\text{s}}$$

with

$$v_{\text{corr}} = V_{\odot} \cdot \cos\theta$$

$$V_{\odot} \approx 370 \text{ km/s}$$

$\theta$  = Angle between the direction of the CMB dipole and the direction to the object

$$\text{Hubble Distance (CMB)} \text{ [Mpc]} = 790.05 \pm 55.30 \quad \rightarrow$$

$$D_c \approx \frac{c_{z,\text{CMB}}}{H_0} \approx \frac{53565 \frac{\text{km}}{\text{s}}}{67.8 \frac{\text{s}}{\text{Mpc}}} \approx 790,04 \text{ Mpc}$$

$$\text{Comoving Distance [Mpc]} \quad D_c(z) = 754.03$$

Due to a redshift greater than 0.1, the **Comoving Distance Formula** based on the **FLRW metric** and the  **$\Lambda$ CDM model** provides more accurate results compared to the simple **Hubble approximation**.

# WHAT DOES THAT MEAN FOR OUR GALAXY?

Name: *WISEA J113253.44+530749.0*



**Hubble Distance** (CMB) [Mpc] = *790.05 ± 55.30*

Distance based on Hubble Approx.  
**(NED Database value)**

→ **2.58 billion light-years**

**Comoving Distance** [Mpc]  $D_c(z) = 754.03$

Distance based on Comoving Distance

→ **2.46 billion light-years**

**2.46 billion light-years** and we can still see the **spiral structure of the galaxy**

# LINKS

**Our website** [www.backyard-universe.de](http://www.backyard-universe.de)

**SimBAD Astronomical Database** <https://simbad.cds.unistra.fr/simbad/>

**NASA Extragalactic Database (NED)** <https://ned.ipac.caltech.edu/>